## Sample Test PS-DIGS W14/15-1

Time 90 minutes

- use of class documents allowed -

Name:

Matr. No.: $\qquad$

Percent:

Grade:
$\qquad$

| 1 | 2 | 3 | 4 | $\Sigma$ |
| :--- | :--- | :--- | :--- | :--- | :--- |

## (1) Conversion of Number Systems and Dual Number Computation

Computation with signed dual number should be carried out. The word size should be 16 bits. The number $x=348_{10}$ is given as a decimal number.
(1.1) What is the minimal (negative) number with 16 bits? Whta is the maximum positive number?
Hint: signed number have a 2's complement representation.
Your results should be given as decimal numbers.
(1.2) Convert the number $x$ into the dual system by sequential division and remainders
(1.3) Wht is the binary number of $-x$ (2's complement, 16 bits!)?
(1.4) Provide the hexadecimal numbers of $x$ und $-x$ ?

## (2) Combinational Logic (Minimization)

The following truth table should be synthesized as combinational gate logic.


| x 3 | x 2 | x 1 | x 0 | y 1 | y 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 | 1 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 0 | 0 |
| 0 | 1 | 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 | 1 | 0 |
| 0 | 1 | 1 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 | 1 |
| 1 | 0 | 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 1 | 1 | 0 |
| 1 | 1 | 0 | 0 | 1 | 1 |
| 1 | 1 | 0 | 1 | 1 | 0 |
| 1 | 1 | 1 | 0 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 0 |

(2.1) Find a minimal solution for the dunction $y_{0}=F_{0}\left(x_{0}, x_{1}, x_{2}, x_{3}\right)$ as product of sums. Draw the circuit with inverters, AND and OR gates.
(2.2) Find a minimal solution for the dunction $y_{1}=F_{1}\left(x_{0}, x_{1}, x_{2}, x_{3}\right)$ as sum of products.
Draw the circuit with inverters, AND and OR gates.

## (3) Hardware State Machine (Moore Machine)

A hardware state machine should be designed to flash an LED several times after a button has beed activated. It should stop after 6 clock cycles. All activities are aligned with the rising edge of the clock signal.


Input of the state machine:
$b \quad '^{\prime}=>$ generate sequences below, ' 0 ' $=>$ off.
Output of the state machine:
led $\quad{ }^{\prime} 1 '=>$ on, ${ }^{\prime} 0 '=>$ off
(3.1) Draw the state diagram.
(3.2) How many states are required; how many flip-flops are required?
(3.3) Design the minimal solution only for $x_{0 \mathrm{n}}$ for the next-state logic (including circuit schematics).
(3.4) Design minimal solution for the output logic.
(3.5) Draw the flip-flops and output logic hardware circuit.

## (4) PicoBlaze Program "Moving Lights"

--- lab (moving light) must be attached to the exam solutions ---

Hints: Your program must contain name and matriculation number The programm should contain comments.

